# Accuracy of Bias Measurements from 3-point Galaxy Correlations

### Kai Hoffmann

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arXiv: 1607.01024, 1503.00313, 1504.02074, 1403.1259



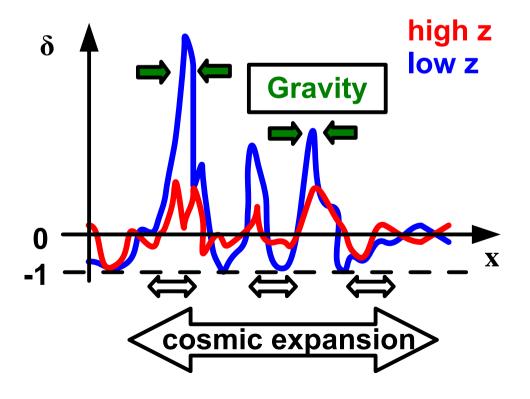


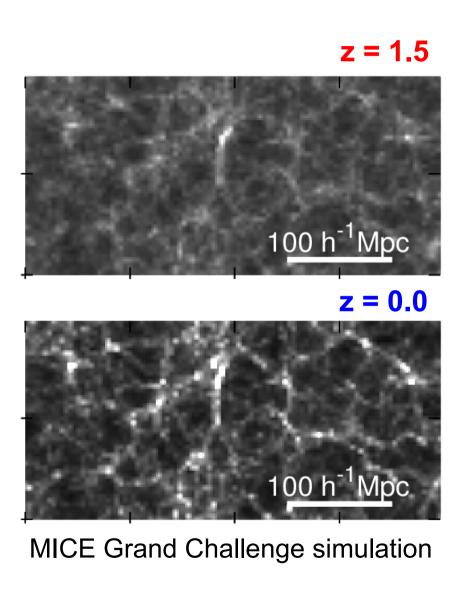
Tsinghua Center for Astrophysics (Beijing)

# growth of matter fluctuations

### matter fluctuations

$$\delta(x) \equiv (\rho(x) - \overline{\rho})/\overline{\rho}$$





# growth depends on cosmology

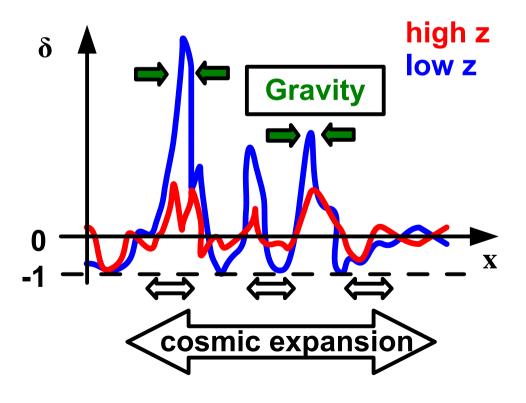
### matter fluctuations

$$\delta(x) \equiv (\rho(x) - \overline{\rho})/\overline{\rho}$$

### linear growth factor

$$D(z) \simeq \delta_m(z) / \delta_m(z_0)$$

(large scale approximation)



### growth sensitive to:

- expansion
- gravity
- matter density
- particle characteristics

# two-point correlation depends on growth

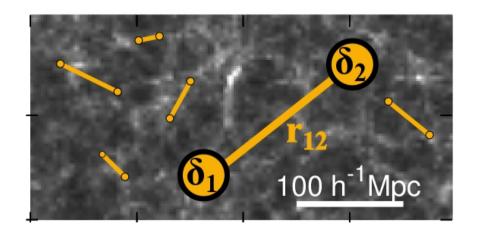
two-point correlation (2pc)

$$\xi(r_{12}) \equiv \langle \delta_1 \delta_2 \rangle(r_{12})$$

linear growth factor

$$D(z) \simeq \delta_m(z) / \delta_m(z_0)$$

(large scale approximation)



- study in 3D config. space
- ξ is isotropic

# cosmology with large-scale structure

two-point correlation (2pc)

linear growth factor

$$\underbrace{\xi(r_{12}) \equiv \langle \delta_1 \delta_2 \rangle(r_{12})}_{\text{(large scale approximation)}} \underbrace{D(z) \simeq \delta_m(z) / \delta_m(z_0)}_{\text{(large scale approximation)}}$$

$$D_0^2(z) \simeq \xi_m(z) / \xi_m(z_0)$$

2pc growth measurement

compare with theory predictions, e.g. ΛCDM (constrain free parameters, discriminate models)

$$D(a) \propto \frac{H(t)}{H(0)} \int_{0}^{a} \frac{da'}{\left[\Omega_{m}/a' + \Omega_{\Lambda}a' - (\Omega_{m} + \Omega_{\Lambda} - 1)\right]^{3/2}} \qquad a \equiv 1/(1+z)$$

# cosmology with large-scale structure

two-point correlation (2pc)

linear growth factor

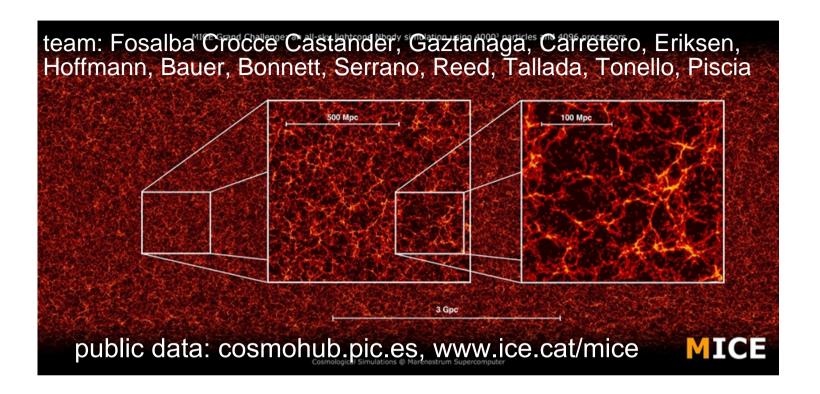
$$\xi(r_{12}) \equiv \langle \delta_1 \delta_2 \rangle(r_{12})$$
 (large scale approximation)

$$D_0^2(z) \simeq \xi_m(z) / \xi_m(z_0)$$

2pc growth measurement

problem: matter 2pc not directly observable!

# MICE Grand Challenge simulation



### MareNostrum super computer

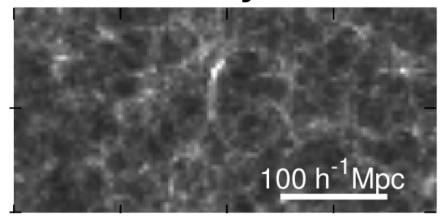


- 4096<sup>3</sup> ( 7 10<sup>10</sup>) particles
- particle mass = 3 10<sup>10</sup> Msun/h
- simulation box (3 Gpc/h)<sup>3</sup>
- ACDM cosmology:

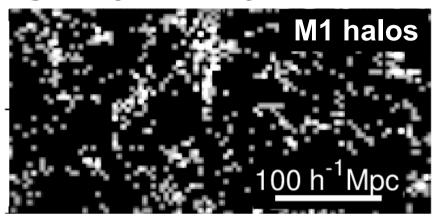
$$\Omega_m = 0.25, \Omega_{\Lambda} = 0.75 \Omega_b = 0.044, \sigma_8 = 0.8 n_s = 0.95, h = 0.7$$

# galaxies trace matter density field

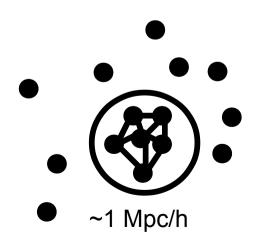
### matter density



galaxy density



# friends-of friends halo detection:

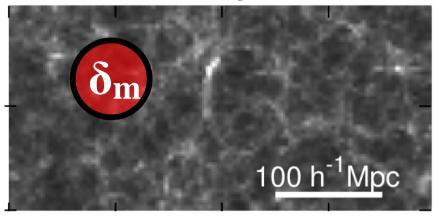


### halo mass samples

sample	mass range [10 <sup>12</sup> M <sub>sun</sub> /h]
MO	0.58 - 2.32
M1	2.32 - 9.26
M2	9.26 - 100
M3	>100

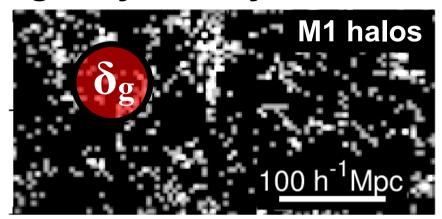
# galaxies bias model

### matter density



galaxy density

0.8



Fry & Gaztanaga (1993)

local quadratic bias model

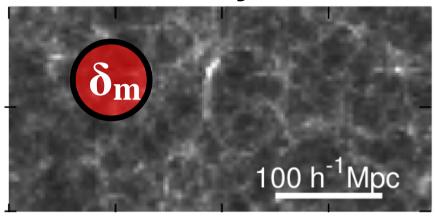
$$\delta_g \simeq b_1 \left[ \delta_m + (c_2/2)(\delta_m^2 - \langle \delta_m^2 \rangle) \right]$$

- $b_1$ : linear bias parameter
- $c_2$ : quadratic bias parameter

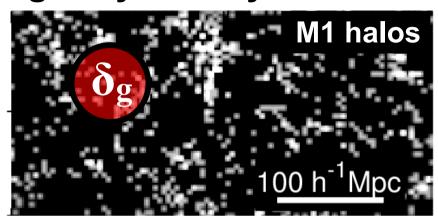
**assumption:**  $\delta_m$  determines  $\delta_g$ 

# galaxies bias model

### matter density



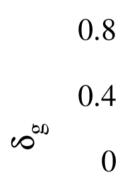
### galaxy density



Fry & Gaztanaga (1993)

### local quadratic bias model

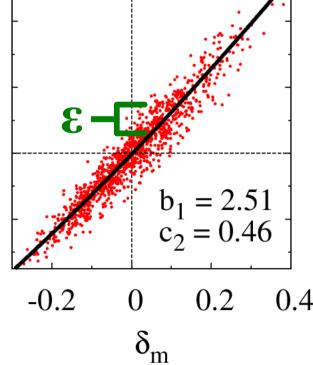
$$\delta_g \simeq b_1 \left[ \delta_m + (c_2/2) (\delta_m^2 - \langle \delta_m^2 \rangle) \right]$$



-0.4

### + E residual from

- stochasticity (e.g. Dekel, Lahav 1999)
- "non-local" contributions (Chan 2012, Baldauf 2012)



# bias in galaxy 2-point correlations

local quadratic bias model

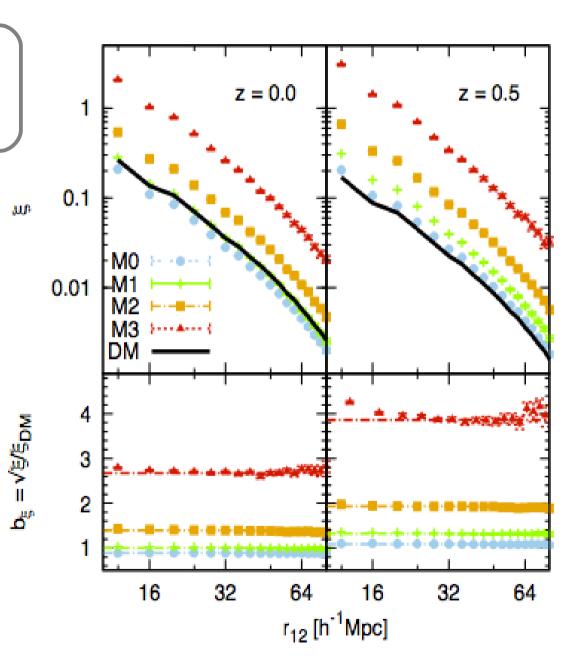
$$\delta_g \simeq b_1 \left[ \delta_m + (c_2/2)(\delta_m^2 - \langle \delta_m^2 \rangle) \right]$$



$$\xi(r_{12}) \equiv \langle \delta_1 \delta_2 \rangle(r_{12})$$

leading order approximation for large scales

$$\xi_g \simeq b_1^2 \xi_m$$

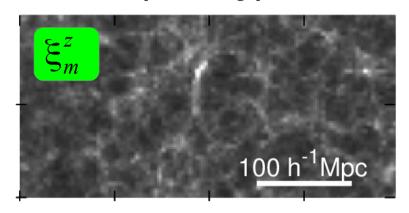


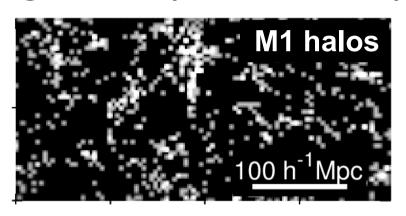
linear bias factor<sup>2</sup> (depends on redshift and halo mass)

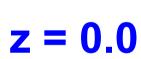
# growth – bias degeneracy

### matter (theory)

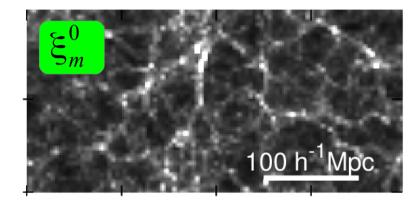
### galaxies (observations)

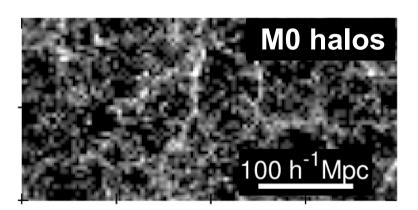






z = 1.0





### linear growth

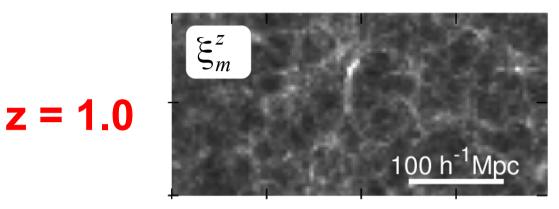
$$D_0(z) = \sqrt{\frac{\xi_m(z)}{\xi_m(0)}}$$

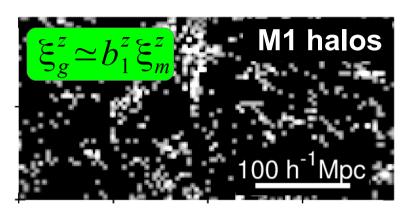
what we would like to observe

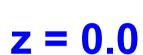
# growth – bias degeneracy

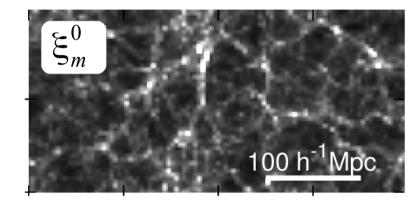
### matter (theory)

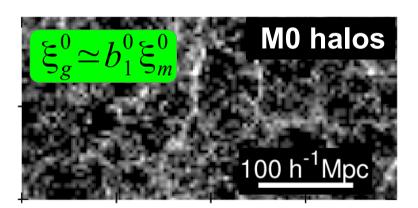
### galaxies (observations)











### linear growth

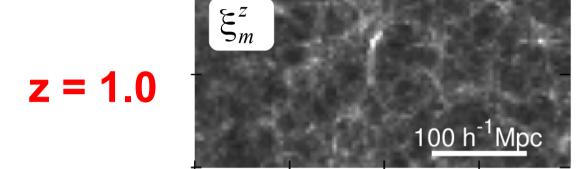
$$D_0(z) = \sqrt{\frac{\xi_m(z)}{\xi_m(0)}} = \frac{b(0)}{b(z)} \sqrt{\frac{\xi_g(z)}{\xi_g(0)}}$$

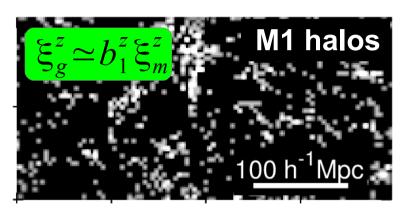
what we can observe

# growth – bias degeneracy

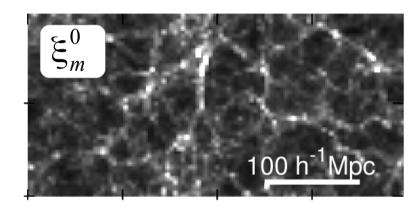
### matter (theory)

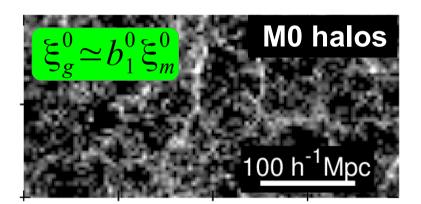
### galaxies (observations)





z = 0.0





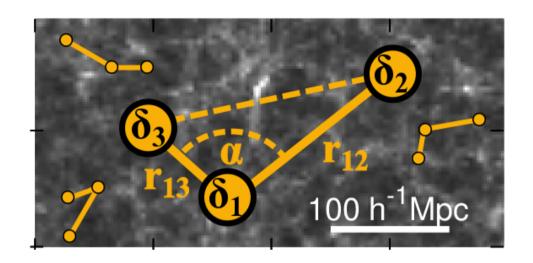
growth-bias degeneracy

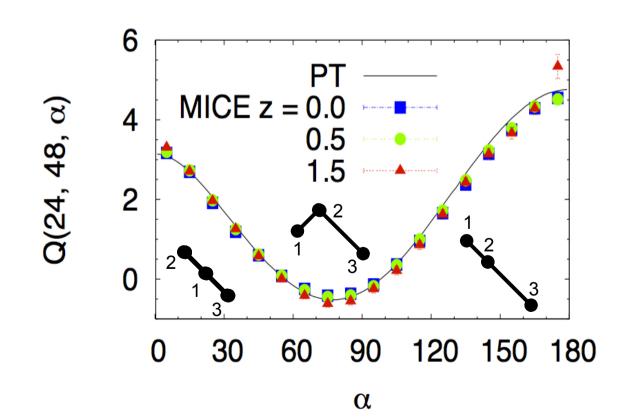
$$D_0(z) \frac{b(z)}{b(0)} = \sqrt{\frac{\xi_g(z)}{\xi_g(0)}}$$

reduced 3-point correlation:

$$Q \equiv \frac{\langle \delta_1 \delta_2 \delta_3 \rangle (r_{12}, r_{13}, \alpha)}{\langle \delta_1 \delta_2 \rangle \langle \delta_1 \delta_3 \rangle + 2 perm.}$$

probes shape of LSS

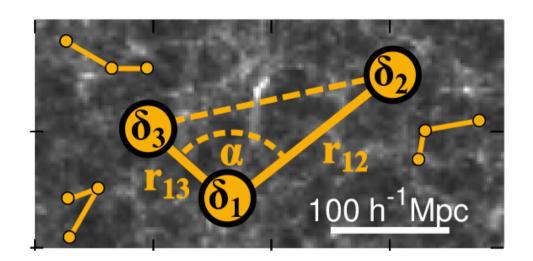


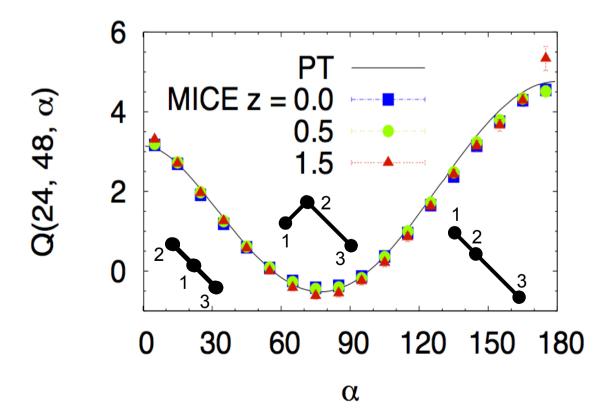


reduced 3-point correlation:

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- probes shape of LSS
- independent of redshift





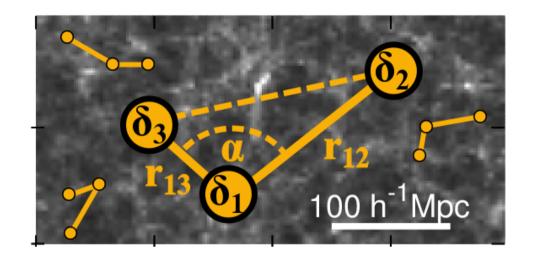
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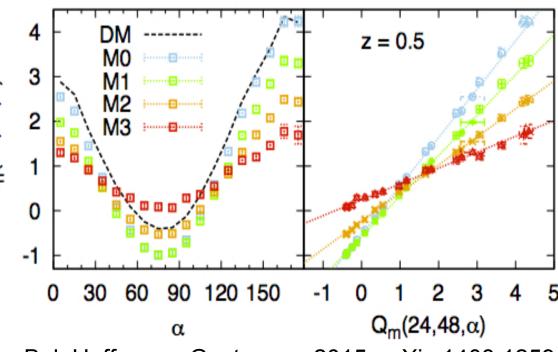
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- probes shape of LSS
- independent of redshift
- depends on bias

$$Q_g \simeq \frac{1}{b_1} (Q_m + c_2)$$

- large scale approximation
- based on local bias model





Bel, Hoffmann, Gaztanaga 2015, arXiv:1403.1259

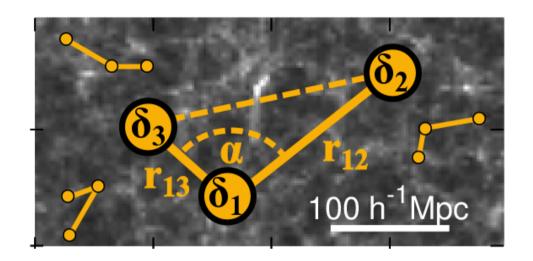
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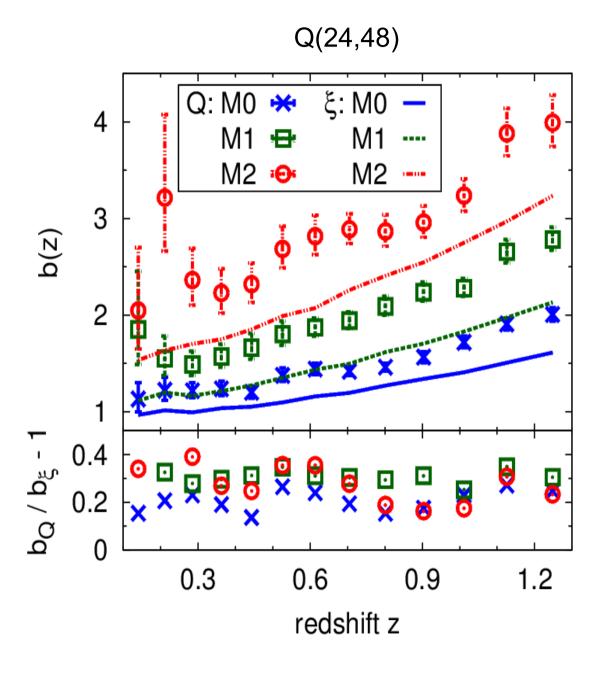


growth - bias degeneracy broken with Q

condition:

$$\frac{b_{\mathcal{Q}}(0)}{b_{\mathcal{Q}}(z)} = \frac{b_{\xi}(0)}{b_{\xi}(z)}$$

# bias from Q ~30% too high



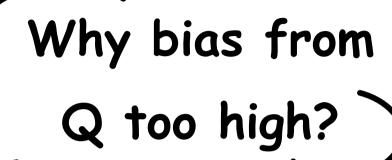
### bias from $\xi$ (lines)

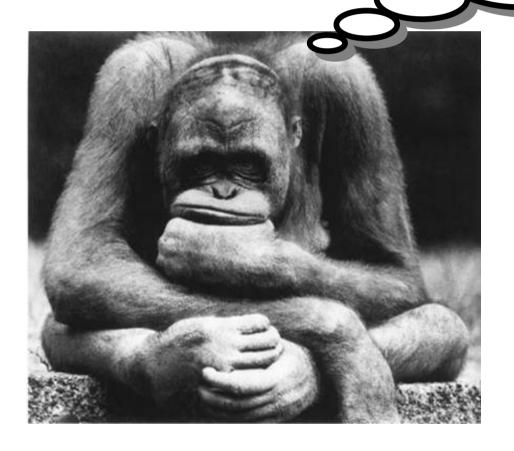
good estimate of linear bias

### bias from Q (symbols)

- ~30 % overestimation
- overestimation similar for different halo mass samples and redshifts
- overestimation appears also very large scales, i.e. Q (36,72)

# bias from Q ~30% too high





- missing higher-order terms in Q<sub>g</sub>?
   (Pollack, Smith & Porciani, 2012)
- non-local bias ? (Chan, Scoccimarro & Sheth, 2012 Baldauf et al. 2012)

### non-local bias

### local quadratic bias model:

$$\delta_g \simeq b_1 \delta_m + (b_2/2)(\delta_m^2 - \langle \delta_m^2 \rangle)$$

### non-local bias

### non-local quadratic bias model:

$$\delta_g \simeq b_1 \delta_m + (b_2/2)(\delta_m^2 - \langle \delta_m^2 \rangle) + (y_2 G_2(\Phi_v))$$

### non-local contributions

$$G_2(\Phi_v) = (\nabla_{ij} \Phi_v)^2 - (\nabla^2 \Phi_v)^2$$

Chan, Scoccimarro & Sheth (2012) Baldauf et al. 2012)

velocity potential:  $\Phi_{\nu}$ 

non-local bias:  $\gamma_2 = g_2 b_1/2$ 

### non-local quadratic bias model

$$\delta_g \simeq b_1 \delta_m + (b_2/2)(\delta_m^2 - \langle \delta_m^2 \rangle) + (g_2/2)(\Phi_v)$$

**Q auto:** galaxy-galaxy-galaxy

$$Q_g \simeq \frac{1}{b_1} (Q_m + [c_2 + g_2 Q_{nloc}])$$

### non-local contributions

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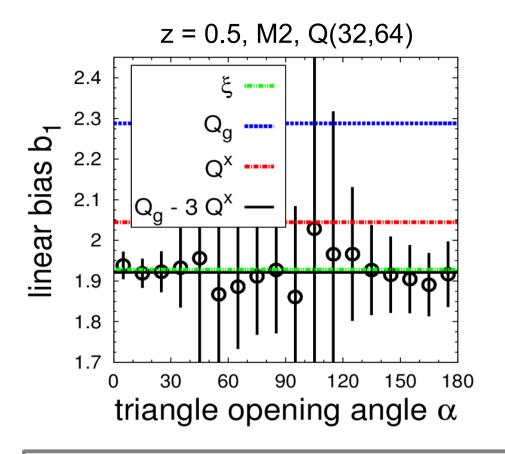
**Q auto:** galaxy-galaxy

$$Q_g \simeq \frac{1}{b_1} (Q_m + [c_2 + g_2 Q_{nloc}])$$

### non-local contributions

Q cross: galaxy-matter-matter

$$Q^{x} \simeq \frac{1}{b_{1}} (Q_{m} + \frac{1}{3} [c_{2} + (g_{2}Q_{nloc})]$$



**Q auto:** galaxy-galaxy-galaxy

$$Q_g \simeq \frac{1}{b_1} (Q_m + [c_2 + g_2 Q_{nloc}])$$

non-local contributions

Q cross: galaxy-matter-matter

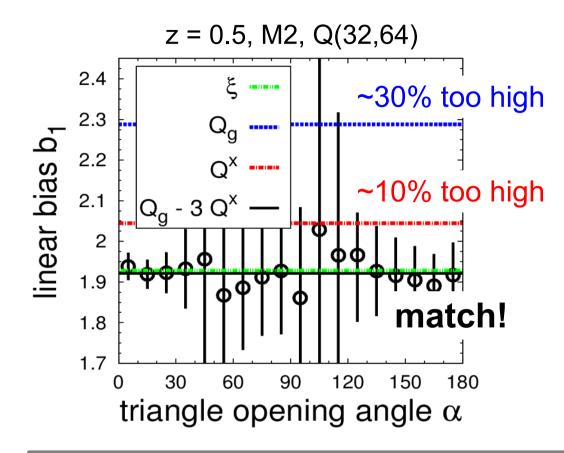
$$Q^{x} \simeq \frac{1}{b_{1}} (Q_{m} + \frac{1}{3}) [c_{2} + g_{2}Q_{nloc}]$$

### **new** linear bias estimator

Q auto – 3 Q cross:

$$b_1 = -2 Q_m / (Q_h - 3 Q^x)$$

- independent of quadratic and non-local contributions  $(c_2 + g_2 Q_{nloc})$
- excellent match with "true" b₁ from ξ
- possible application in galaxy-lensing cross-correlation



**Q auto:** galaxy-galaxy-galaxy

$$Q_g \simeq \frac{1}{b_1} (Q_m + [c_2 + g_2 Q_{nloc}])$$

non-local contributions

Q cross: galaxy-matter-matter

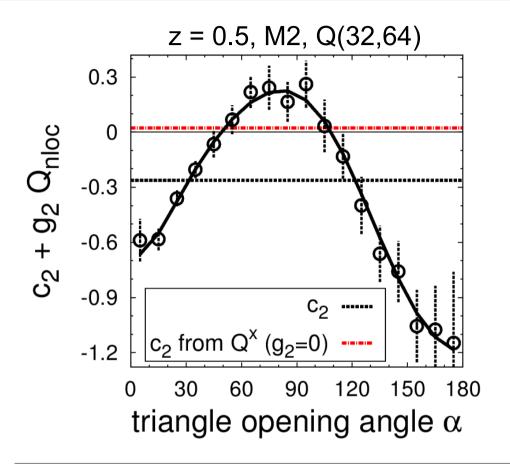
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**Q auto:** galaxy-galaxy

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### non-local contributions

Q cross: galaxy-matter-matter

$$Q^{x} \simeq \frac{1}{b_{1}} (Q_{m} + \frac{1}{3} [c_{2} + g_{2}Q_{nloc}]$$

### Q auto - Q cross:

$$b_{\xi}(3/2)(Q_h - Q^x) = c_2 + g_2 Q_{nloc}$$

- independent of  $Q_m$
- depends on triangle configuration
  - local quadratic bias model  $(g_2 = 0)$  fails
- agreement with  $Q_{nloc}$  prediction
- can be used to measure  $c_2$  and  $g_2$

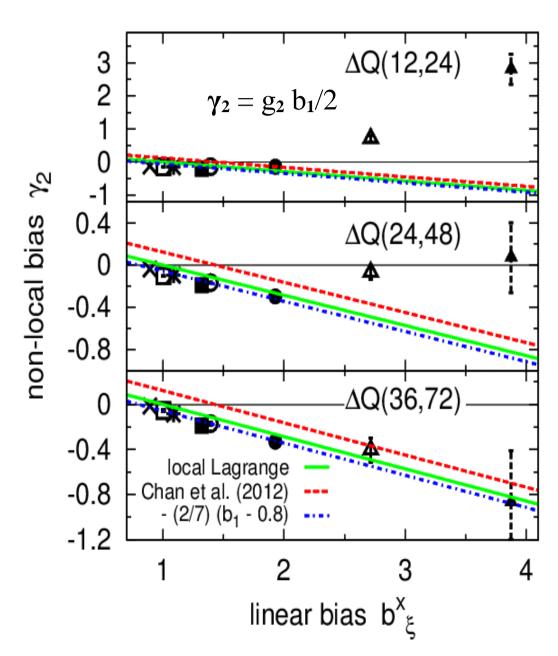
### symbols:

• measurements from  $\Delta Q = Q - Q^X$ 

#### lines:

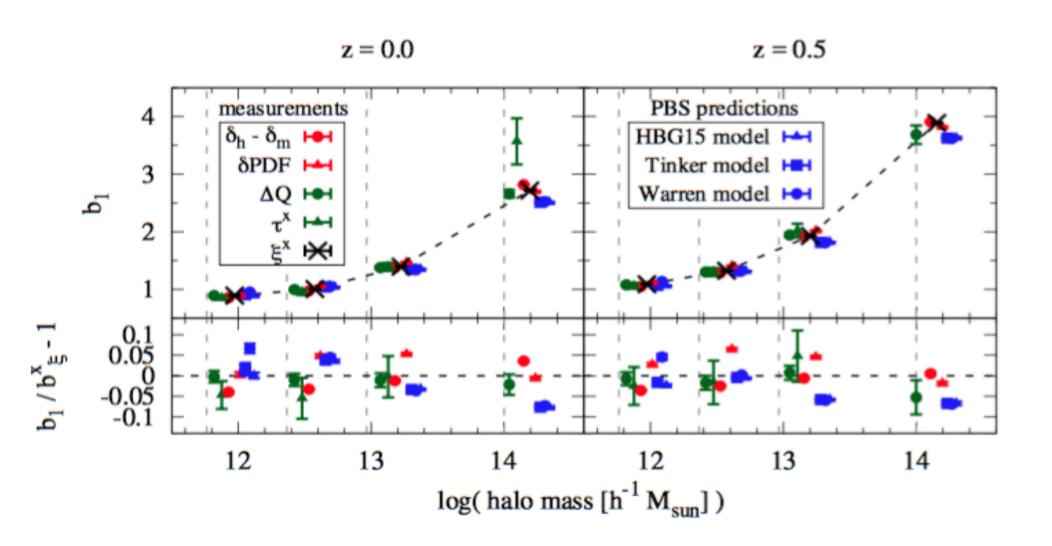
- fit to measurements
- local Lagrangian prediction
- fit from Chan, Scoccimarro, Sheth (2012)
- strong scale dependence of non-local bias  $\gamma_2 = g_2 b_1/2$
- at r > 35 Mpc/h
  - b<sub>1</sub>-γ<sub>2</sub> linear
  - close to local lagrangian model

$$g_2 = -(4/7)(1-b_1^{-1})$$



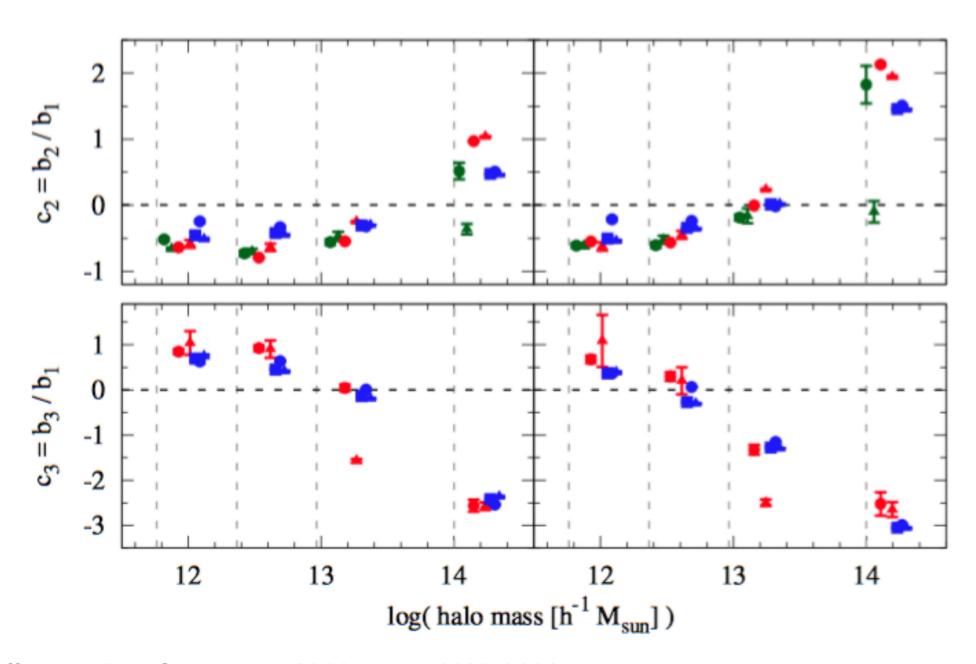
Hoffmann, Bel, Gaztanaga 2015, arXiv:1504.02074

# linear bias comparison



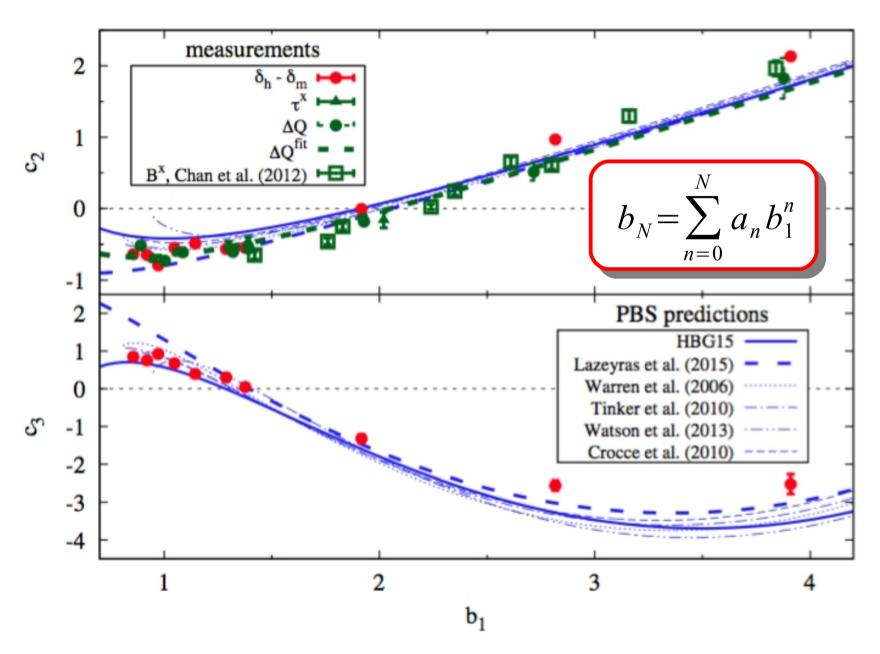
Hoffmann, Bel, Gaztanaga 2016, arXiv:1607.01024

# non-linear bias comparison



Hoffmann, Bel, Gaztanaga 2016, arXiv:1607.01024

### universal relation between b1, b2, b3



Hoffmann, Bel, Gaztanaga (2015, 2016, arXiv:1503.00313, 1607.01024)

# b1 constraints from observed 3pc

### measurement

$$Q_h \simeq \frac{1}{b_1} \left( Q_m + [c_2 + g_2 Q_{nloc}] \right)$$
model

#### model

- Qm & Qnloc from leading order perturbation theory
- c2 from (universal) c2(b1) relation (Hoffmann, Bel, Gaztanaga 2015)  $c_2 = 0.77b_1^{-1} 2.43 + b_1$
- g2 from local Lagrangian bias model  $g_2 = -(4/7)(1-b_1^{-1})$

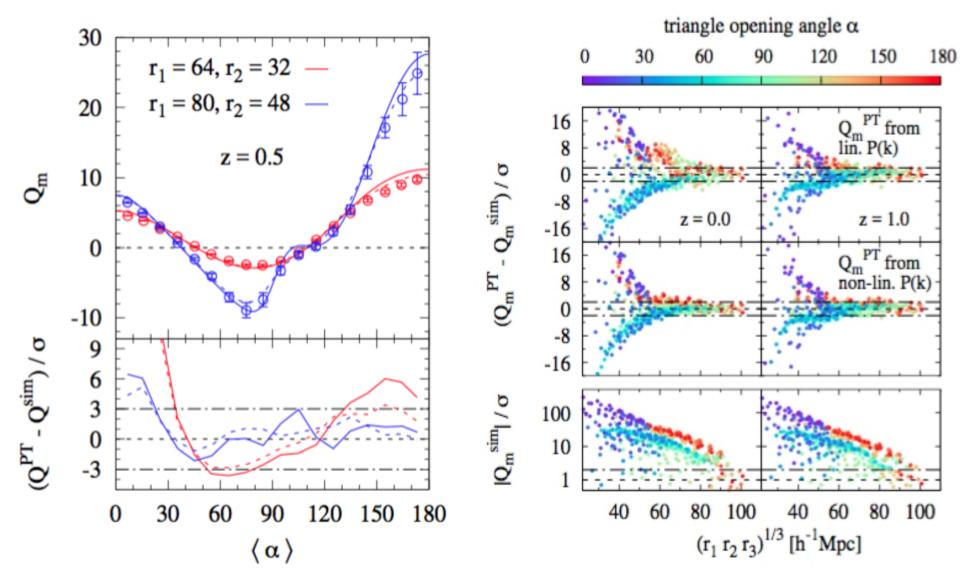
### for measuring b1 from 3pc in surveys we would like to know:

- can b1 c2 and b1-g2 relations be used to reduce
- number of free bias parameters (=> reduce error on b1)?
- at which scales is PT valid?
- consistent results in config. and Fourier space?

### Hoffmann, Gaztanaga, Scoccimarro, Crocce in prep.:

• 49 N-body sims, 1280 (Mpc/h)^3, 3pc for 504 triangles

# matter 3pc: PT vs simulation



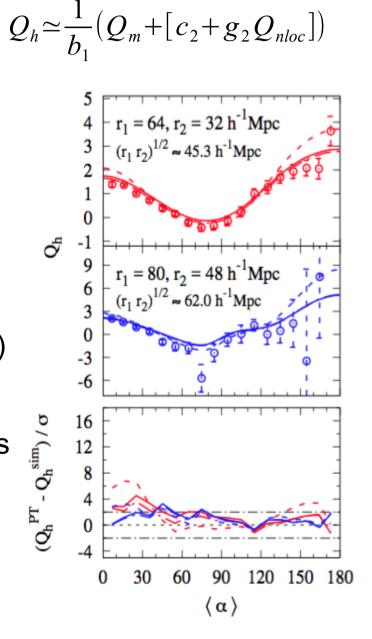
- Qm predictions from leading order perturbation theory
- 2 sigma agreement with measurements for (r1r2r3)^1/3 > 60
- prediction improve when using non-lin Pk

# halo 3pc: PT vs simulation

### halo-halo-halo

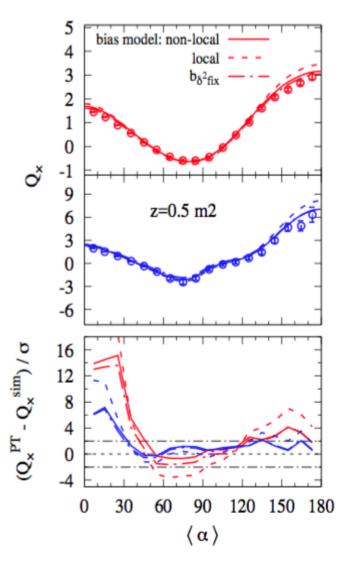
# models: $O_b \simeq \frac{1}{1} (O_m + [O_m])$

- Qm & Qnloc from leading order PT
- local bias model (g2=0, dashed) fails
- c2(b1) and g2(b1) relations (dasheddotted) work!

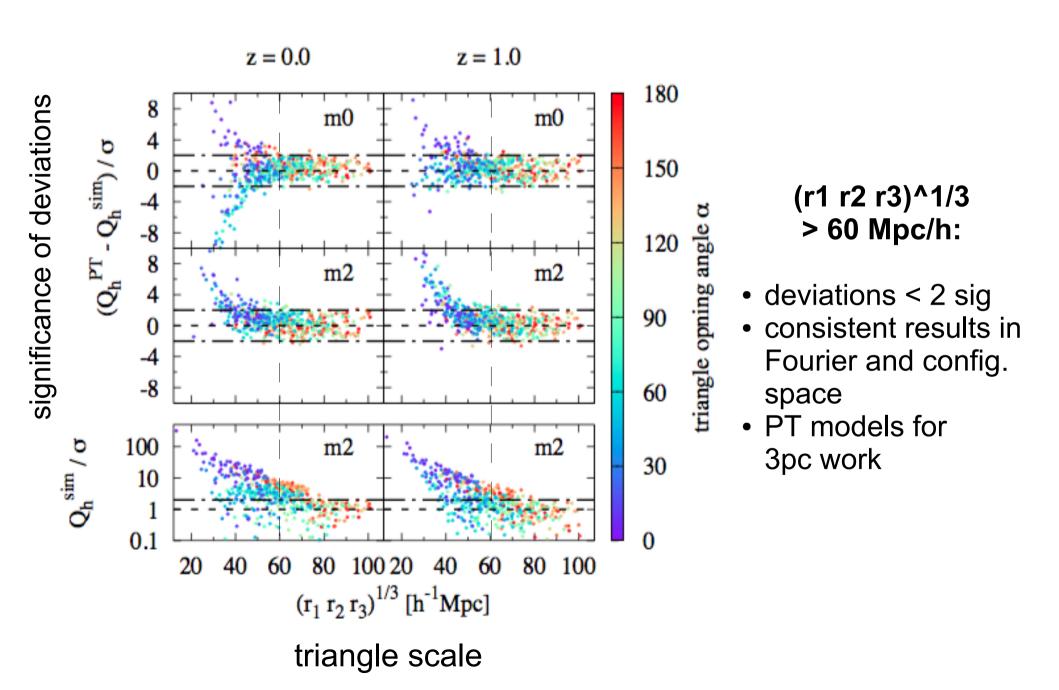


### halo-matter-matter

$$Q_x \simeq \frac{1}{b_1} (Q_m + \frac{1}{3} [c_2 + g_2 Q_{nloc}])$$



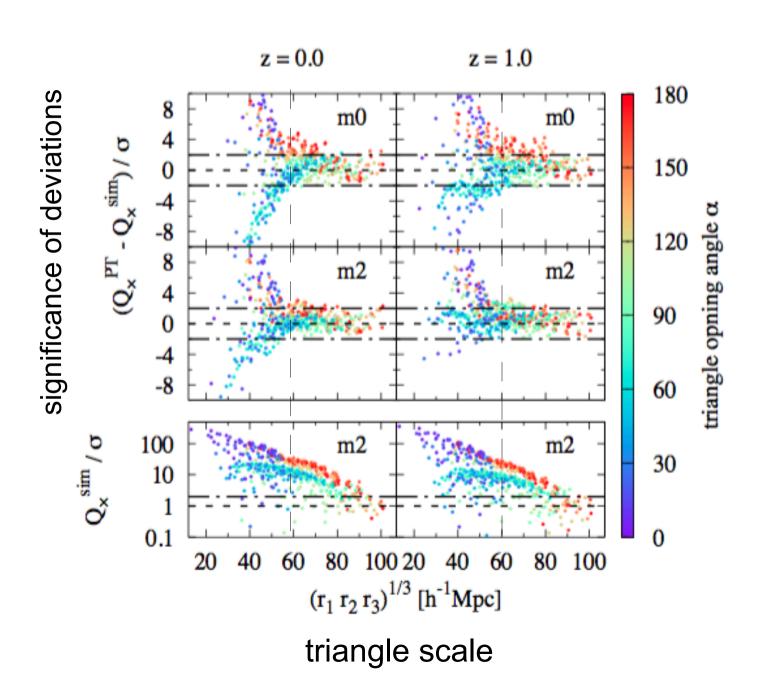
# halo-halo 3pc: PT vs simulation



### Conclusions

- constraints on cosmological models limited by growth-bias degeneracy
- growth—bias degeneracy broken with 3pc
- 3pc is affected by non-local contributions to bias function
- agreement with Fourier space results only at > 60 Mpc/h
- nearly universal relation between b2(b1) and b3(b1) can be used to decrease error on b1 from 3pc

# halo-matter-matter 3pc: PT vs simulation



# constraining lin bias (b1) with 3pc

non-local quadratic 3pc model

$$Q_h \simeq \frac{1}{b_1} (Q_m + [c_2 + g_2 Q_{nloc}])$$



$$c_2 = 0.77b_1^{-1} - 2.43 + b_1$$

(roughly) universal b1 - c2 relation (Hoffmann, Bel, Gaztanaga 2015)

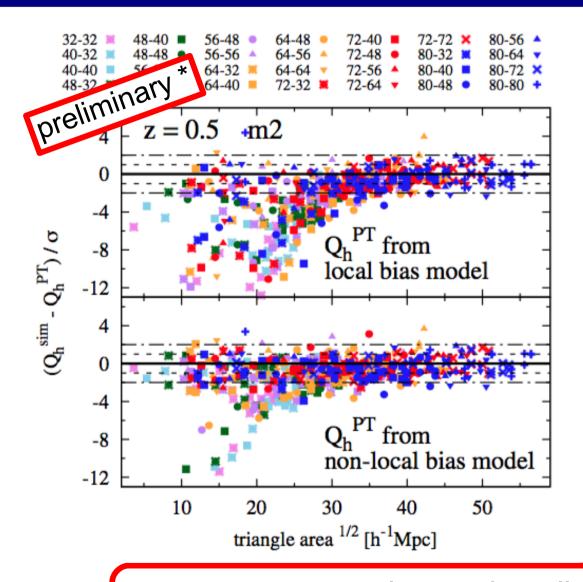
$$g_2 = -(4/7)(1-b_1^{-1})$$

local Lagrangian bias model

### questions concerning an application in observations

- can b1 c2 and b1-g2 relations be used to reduce Nr. of free bias parameters (=> reduce error on b1)?
- at which scales is PT valid?

# 3pc in Fourier and config. space



measurement

$$Q_h \simeq \frac{1}{b_1} (Q_m + [c_2 + g_2 Q_{nloc}])$$
model

- Qm & Qnloc from leading order perturbation theory
- b1, c2, g2 from Fourier space measurements using the same simulations (Chan, Sheth, Scoccimarro, 2012)

- measurements better described by non-local model
- convergence between 30-40 Mpc/h

<sup>\*</sup>Hoffmann, Gaztanaga, Scoccimarro, Crocce in prep.